

A Simple, Accurate Capacitance-Voltage Model of Undoped Silicon Nanowire MOSFETs

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May 6, 2009

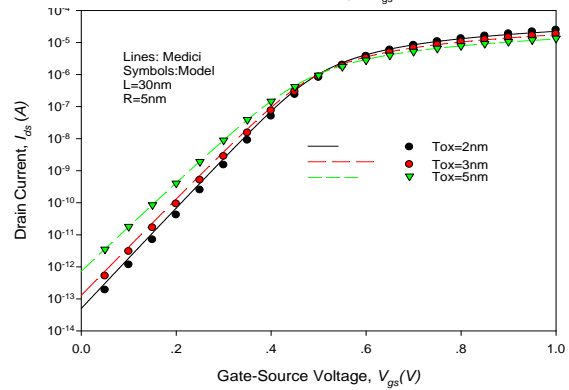
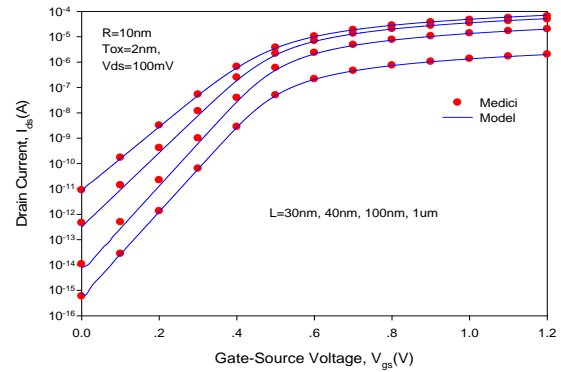
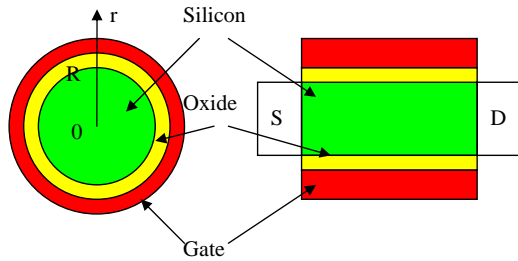


Overview

- Motivation
- Model Equation
- Simulation Results & Verification
- Conclusion



SiNW MOSFETs



Modeling Capacitances in FET

- Intrinsic Capacitances, Extrinsic Capacitances
- Simple
- Accurate, Valid in all region
- Symmetry

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Surface Potential Solution

$$\frac{d^2\phi}{dr^2} + \frac{1}{r} \frac{d\phi}{dr} = \frac{qn_i}{\epsilon_{Si}} e^{(\phi - V_C)/v_{th}} \quad V_{GF} = \phi_s + \frac{4\epsilon_{si}v_{th}}{RC_{ox}} \left(\frac{\delta R^2 e^{\frac{\phi_s - V_C}{v_{th}}}}{-4 + 2\sqrt{4 + 2\delta R^2 e^{\frac{\phi_s - V_C}{v_{th}}}}} - 1 \right)$$

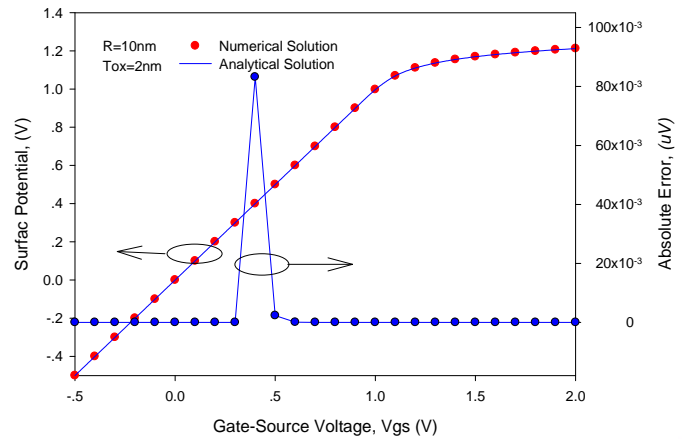
$$\phi_{s1} \approx V_{gf} - \frac{4\epsilon_{si}v_{th}}{RC_{ox}} \left(\frac{\delta R^2 \left(1 + \frac{V_{gf}}{v_{th}} \right)}{-4 + 2\sqrt{4 + 2\delta R^2 \left(1 + \frac{V_{gf}}{v_{th}} \right)}} - 1 \right)$$

$$\phi_{s2} \approx v_{th} \ln \left(\frac{8 \cdot \frac{4\epsilon_{si}v_{th}}{RC_{ox}} \cdot V_{GF} \left(\frac{4\epsilon_{si}v_{th}}{RC_{ox}} \cdot V_{GF} + 1 \right)}{\delta R^2} \right)$$

$$\phi_{s3} = \frac{1}{2} \left(\phi_{s2} + \phi_{s1} - \sqrt{(\phi_{s2} - \phi_{s1})^2 - d} \right)$$

$$\phi_{s4} \approx v_{th} \ln \left(\frac{8 \cdot \frac{4\epsilon_{si}v_{th}}{RC_{ox}} \cdot (V_{GF} - \phi_{s3}) \left(\frac{4\epsilon_{si}v_{th}}{RC_{ox}} \cdot (V_{GF} - \phi_{s3}) + 1 \right)}{\delta R^2} \right)$$

$$\phi_{s5} = \frac{1}{2} \left(\phi_{s4} + \phi_{s1} - \sqrt{(\phi_{s4} - \phi_{s1})^2 - d} \right)$$



$$\phi_s = \phi_{s5} + K - \frac{f_2}{2f_1} K^2 + \frac{(3f_2)^2 - f_1f_3}{6(f_1)^2} K^3 + \frac{10f_1f_2f_3 - (f_1)^2 f_4 - 15(f_2)^3}{24(f_1)^3} K^4$$

Charge Equation

- Gate Charge

$$Q_G = 2\pi R \int_0^L Q_G(y) dy$$

- Source and Drain Charge (Ward-Dutton method)

$$Q_S = 2\pi R \int_0^L \left(1 - \frac{y}{L}\right) Q_i(y) dy$$

$$Q_D = 2\pi R \int_0^L \frac{y}{L} Q_i(y) dy$$

- Capacitance

$$C_{ij} = \delta_{ij} \frac{\partial Q_i}{\partial V_j} \quad \delta_{ij} = \begin{cases} 1, & i = j \\ -1, & i \neq j \end{cases}$$



Current Expressions

- Current Equation

$$I_{ds} = \mu \frac{2\pi R}{L} \int_{\phi_s(0)}^{\phi_s(L)} (-Q_{sc}) \frac{dV}{d\phi_s} d\phi_s \quad \frac{dV_C}{d\phi_s} = 1 + v_{th} \cdot \left(\frac{1}{V_{GF} - \phi_s} + \frac{1}{V_{GF} - \phi_s + C_R} \right)$$

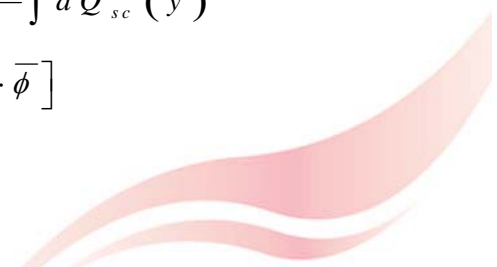
$$= \mu C_{ox} \frac{2\pi R}{L} \left\{ V_{gf} \Delta\phi - \bar{\phi}_s \Delta\phi + v_{th} \left[2\Delta\phi + C_R \ln \left(\frac{V_{gf} - \phi_s(L) + C_R}{V_{gf} - \phi_s(0) + C_R} \right) \right] \right\}$$

- Approximate Current Equation

$$I_{ds} = 2\pi R \mu Q_{sc}(y) \frac{dV_C}{dy} \quad \frac{dV_C}{d\phi_s} \approx 1 + v_{th} \cdot \frac{1}{V_{GF} - \phi_s}$$

$$\approx -\mu \frac{2\pi R}{L} \int Q_{sc}(y) d\phi_s + \mu v_{th} \frac{2\pi R}{L} \int dQ_{sc}(y)$$

$$= \mu \frac{2\pi R C_{ox}}{L} \left[(V_{gf} + v_{th}) \cdot \Delta\phi - \Delta\phi \cdot \bar{\phi} \right]$$



y Expression

- It is derived based upon current

$$y = \frac{2\pi R\mu}{I_{ds}} \int_{V_s}^V Q_{sc}(y) dV_C$$

$$= \frac{L}{\left[(V_{gf} + 2v_{th}) - \bar{\phi}_s \right] \Delta\phi} \left[(V_{gf} + 2v_{th}) - \bar{\phi}_s \right] \Delta\phi'$$

- Taylor's expansion

$$y \approx \frac{L}{2} \left(1 + \frac{\Delta\phi}{4H} \right) + \frac{L}{\Delta\phi} (\phi_s - \bar{\phi}_s) + \frac{L}{\Delta\phi H} \frac{(\phi_s - \bar{\phi}_s)^2}{2}$$

$$= \frac{L}{2} \left(1 + \frac{\Delta\phi}{4H} \right) + \frac{L}{\Delta\phi} \left(u - \frac{u^2}{2H} \right)$$



Terminal Charge

- Gate Charge

$$Q_G = 2\pi R \int_0^L Q_G(y) dy$$

$$= 2\pi R C_{ox} L \left[(V_{gf} - \bar{\phi}_s) + \frac{\Delta\phi^2}{12H} \right]$$

- Drain Charge

$$Q_D = 2\pi R \int_0^L \frac{y}{L} Q_i(y) dy$$

$$= \pi R C_{ox} \cdot \left[-\frac{L}{H^2} \frac{\Delta\phi^3}{80} - \frac{-y_m \Delta\phi^2 + \Delta\phi \cdot L (V_{gf} - \bar{\phi}_s)}{6H} \right]$$

$$= \pi R C_{ox} \cdot \left[-\frac{\Delta\phi L}{6} \left(1 + \frac{(V_{gf} - \bar{\phi}_s)}{2H} \right) + 2y_m (V_{gf} - \bar{\phi}_s) \right]$$

- Source

$$Q_S = 2\pi R \int_0^L \left(1 - \frac{y}{L} \right) Q_i(y) dy$$

$$= Q_G - Q_D$$



Short-Channel Effects

- Short-Channel Current

$$I_{ds} \approx \frac{\mu_s 2\pi RC_{ox} [(V_{gf} + 2v_{th}) - \bar{\phi}_s] \Delta\phi}{L + \frac{\delta_L \Delta\phi}{E_{sat}} + R_{sd} \mu_s 2\pi RC_{ox} [(V_{gf} + 2v_{th}) - \bar{\phi}_s]}$$

- Terminal Charge

$$y \approx \frac{L}{2} \left(1 + \frac{\Delta\phi}{4H^*} \right) + \frac{L}{\Delta\phi} \left(u - \frac{u^2}{2H^*} \right)$$

$$Q_G = 2\pi RC_{ox} L \left[(V_{gf} - \bar{\phi}_s) + \frac{\Delta\phi^2}{12H^*} \right]$$

$$Q_D = \pi RC_{ox} \left[\begin{aligned} & -\frac{L}{H^{*2}} \frac{\Delta\phi^3}{80} - \frac{-y_m \Delta\phi^2 + \Delta\phi \cdot L (V_{gf} - \bar{\phi}_s)}{6H^*} \\ & -\frac{\Delta\phi L}{6} \left(1 + \frac{(V_{gf} - \bar{\phi}_s)}{2H^*} \right) + 2y_m (V_{gf} - \bar{\phi}_s) \end{aligned} \right]$$

$$Q_S = Q_G - Q_D$$

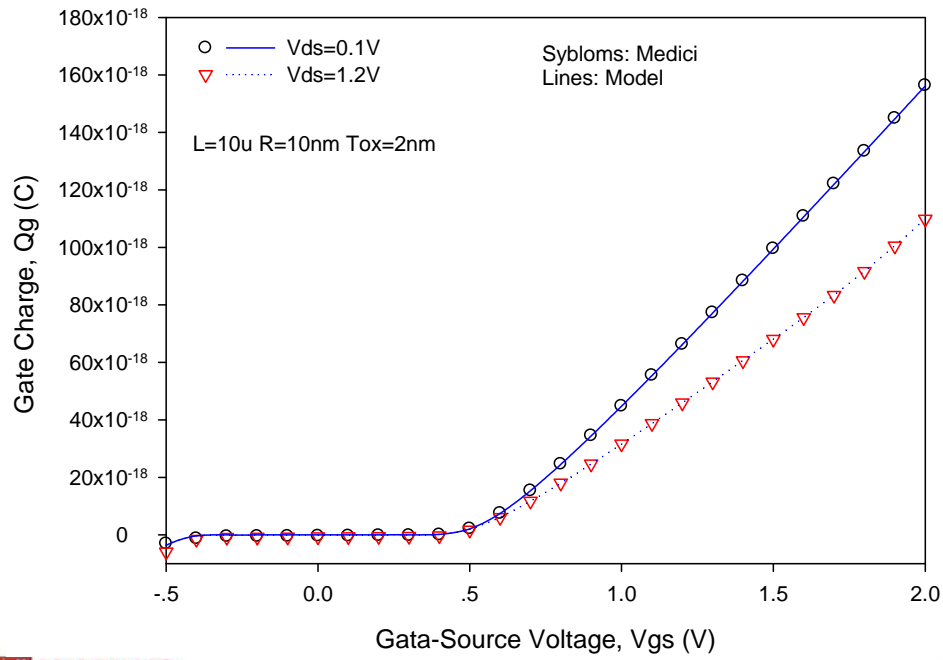


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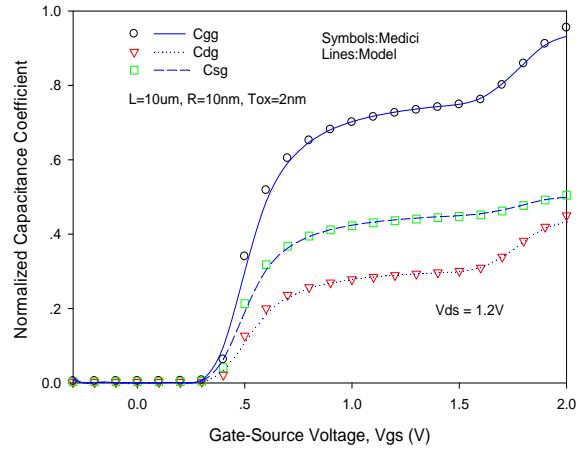
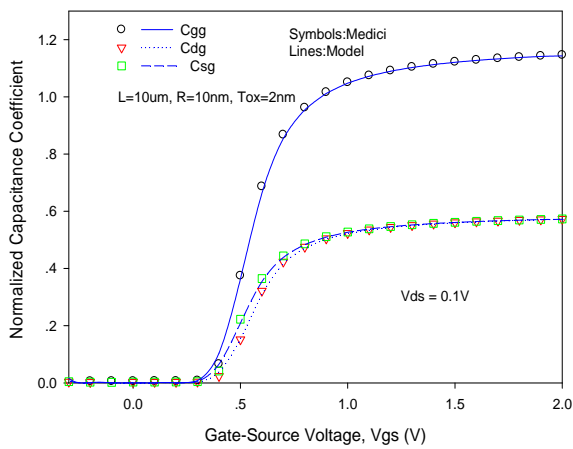
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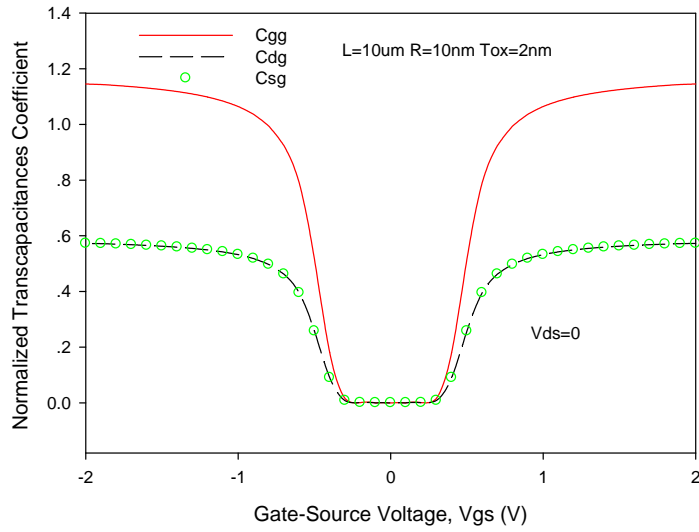
Charge Verification



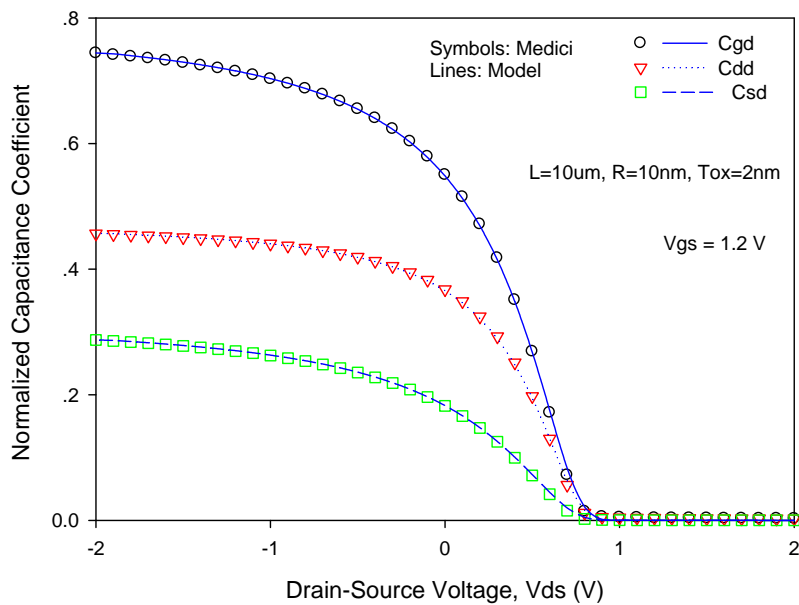
Cxg Verification



Symmetry of C_{xg}



C_{xd} Verification



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Conclusion

- An approximate current equation is developed
- A simple charge model is derived based upon the approximate current equation
- Accurate and valid in all region



Thank You!

