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# LINFET: A BSIM Class FET Model with Smooth Derivatives at $V_{ds}=0$

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## Toy Model

### Original

- Variables:  $V_{gs}, V_{ds}$
- Parameters:  $V_t, \mu$

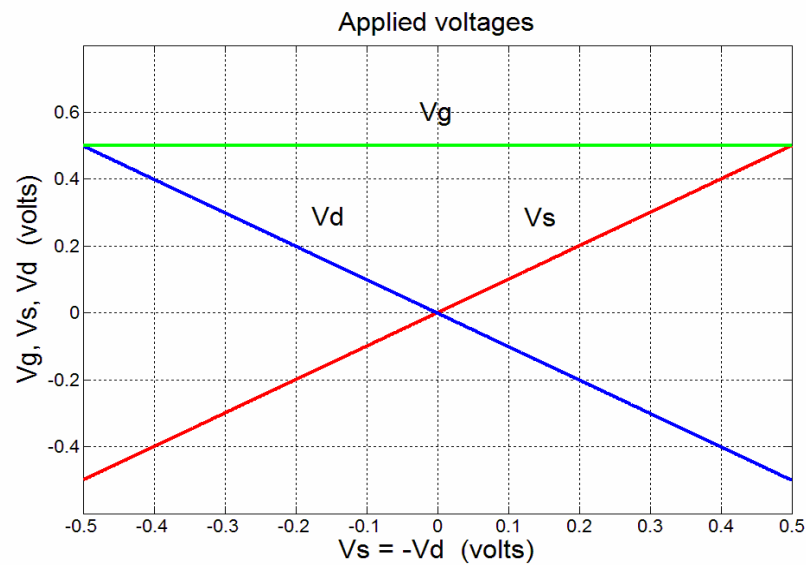
$$J_{ds} = \frac{2WC_{ox}\mu}{L} \left( V_{gst} - \frac{V_{ds}}{2} \right) V_{ds}$$

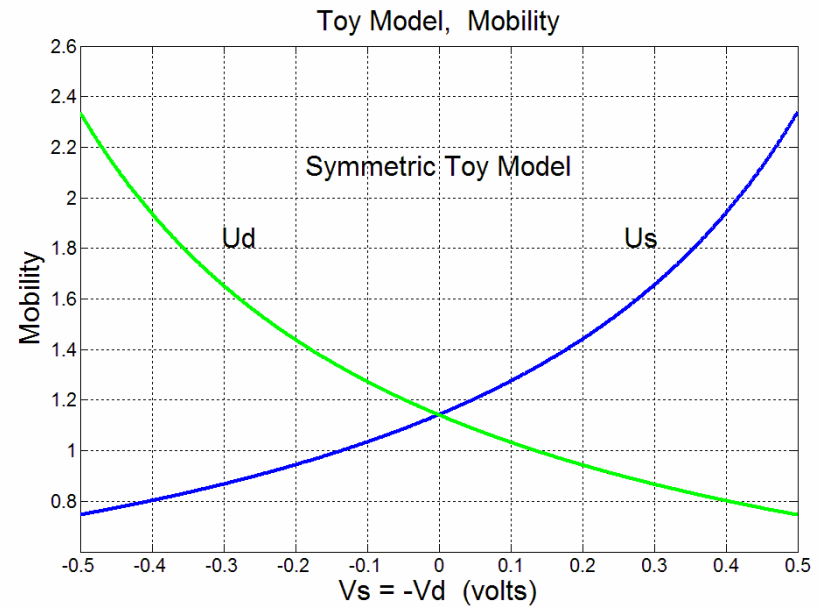
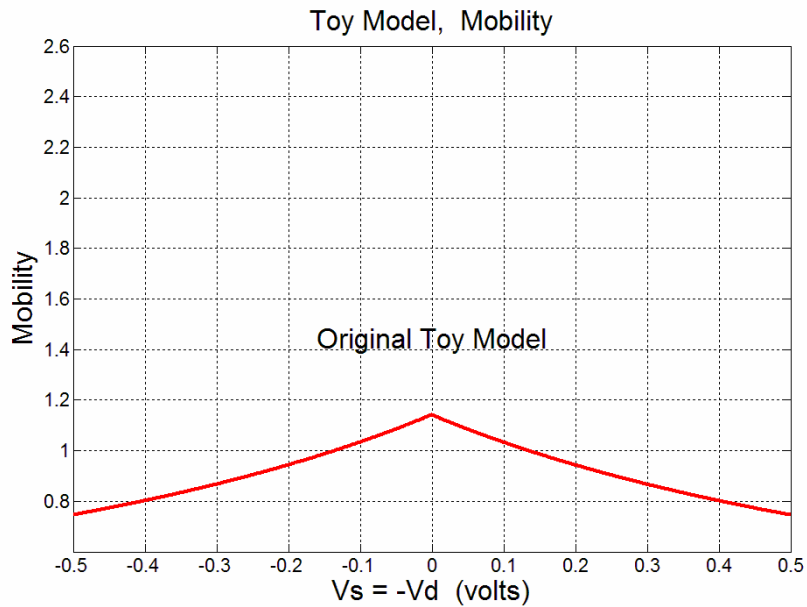
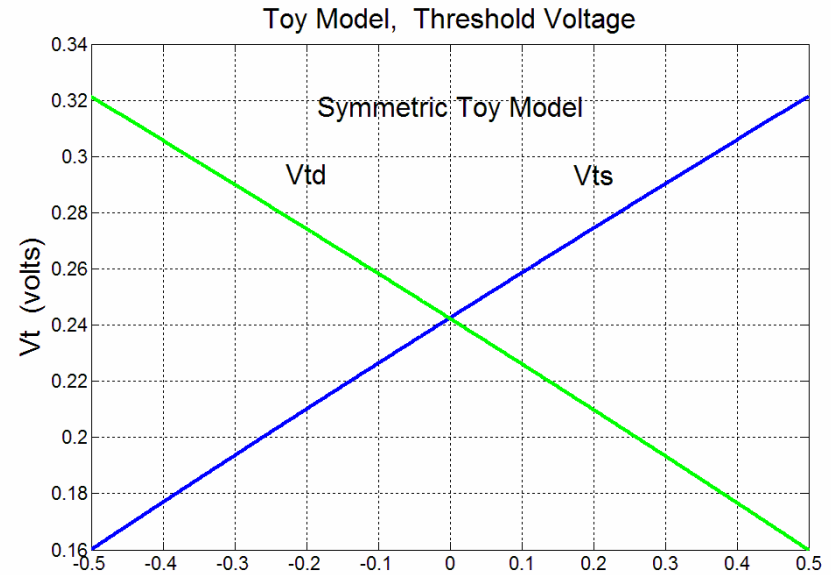
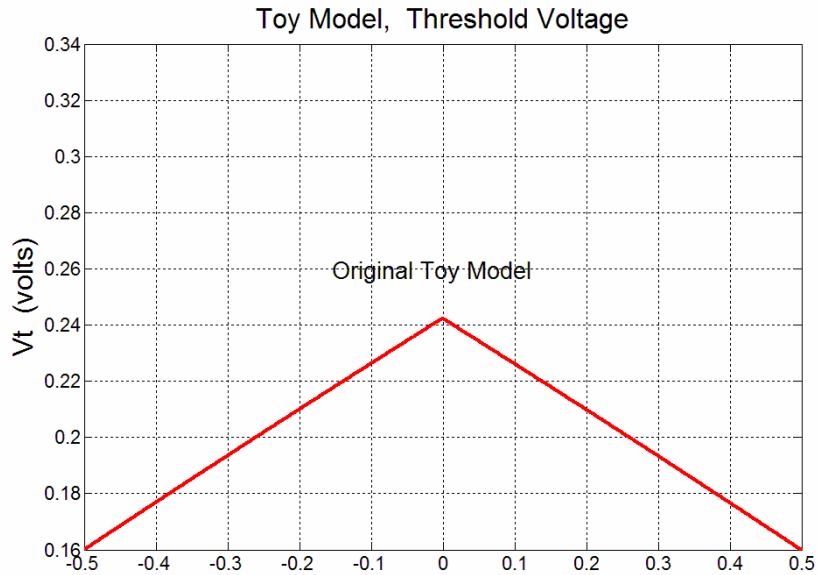
$$(V_{ds} \geq 0)$$

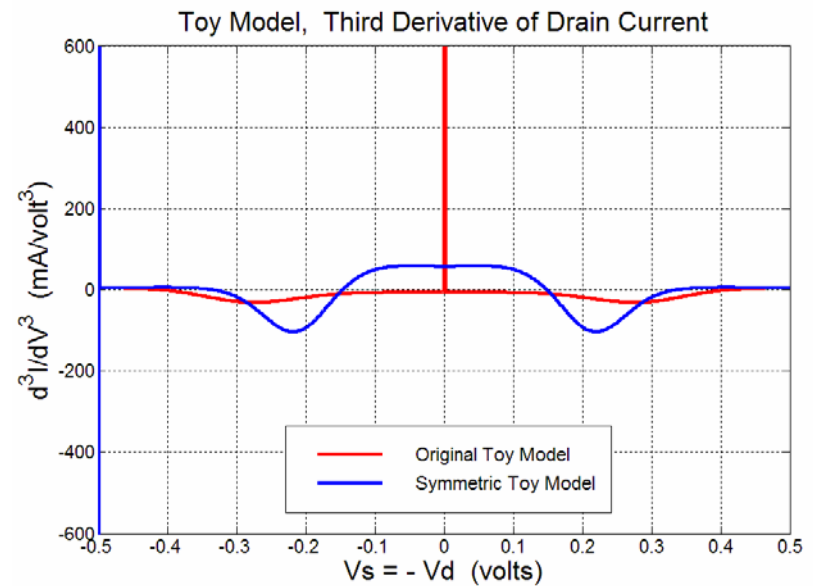
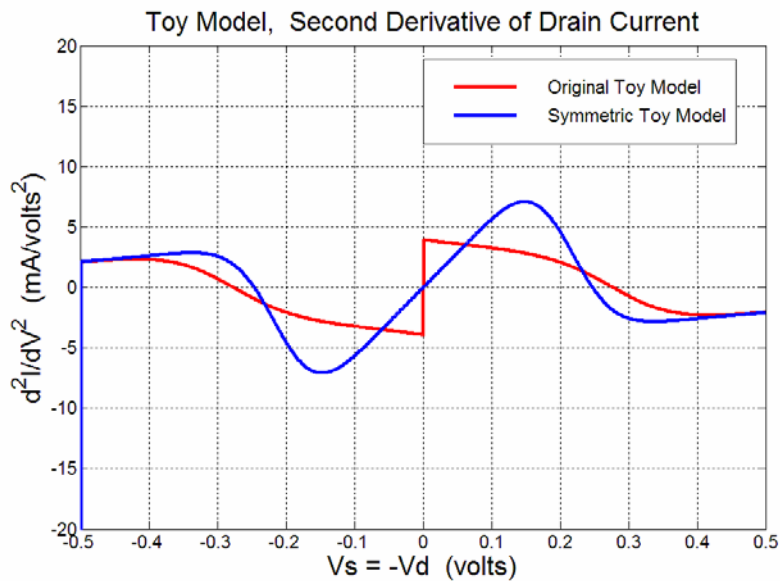
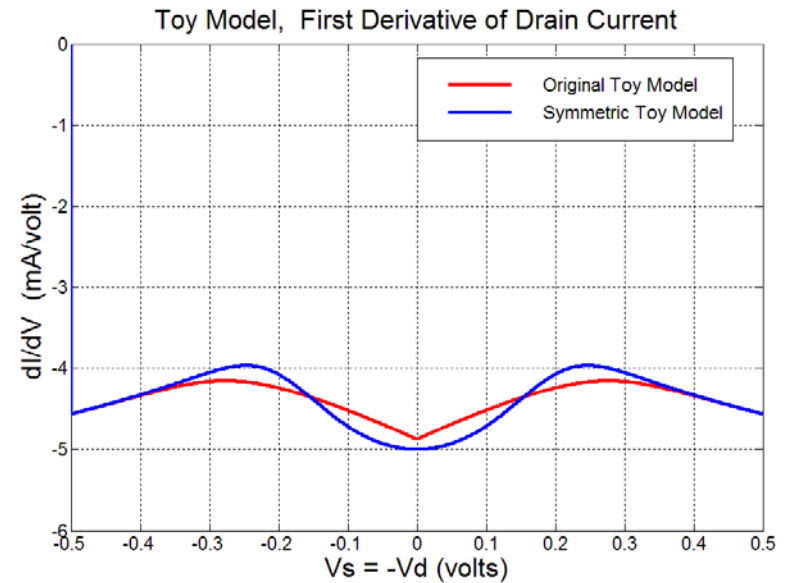
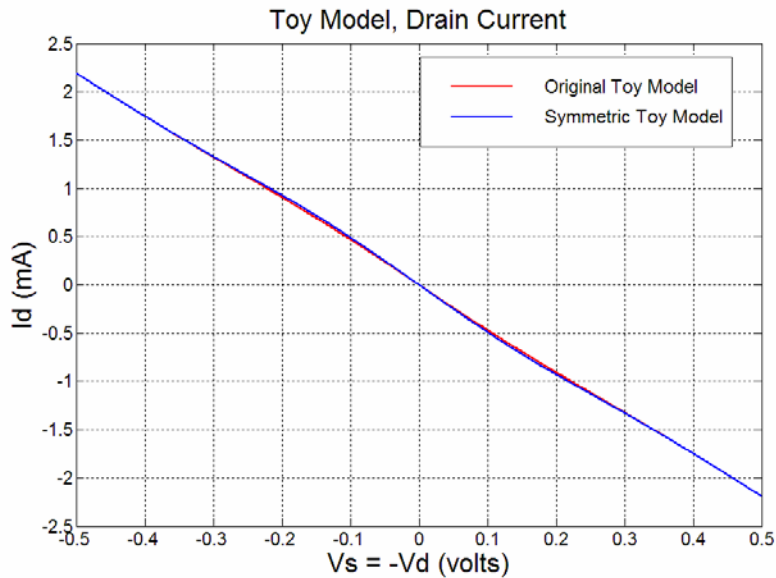
### Symmetric

- Variables:  $V_{gs}, V_{gd}$
- Parameters:  $V_{ts}, V_{td}, \mu_s, \mu_d$

$$J_{ds} = \frac{WC_{ox}}{L} \left( \mu_s V_{gst}^2 - \mu_d V_{gdt}^2 \right)$$







## Introduction

- **The linearity of a compact transistor model at or near  $V_{ds}=0$  is important for the design of RF circuits such as mixers and switches.**
- **Currently established compact FET models such as BSIM3/4, and others have traditionally had problems around this bias point.**
- **In this paper we show how discontinuities in the derivatives of the drain current and charges arise in the threshold based BSIM model, and a method of fixing them is suggested.**

## Derivation of the intrinsic BSIM model

- Channel charge

$$\begin{aligned} q_g(y) &= -q_c(y) - q_b(y) = \varepsilon_{si} E_{si} = \varepsilon_{ox} E_{ox} \\ &= C_{ox} (\psi_g - \psi_c(y)) \approx C_{ox} (V_g - V_c(y) - V_{t0}) \end{aligned}$$

- Bulk charge linearized

$$\begin{aligned} -q_b(y) &= \sqrt{2q\varepsilon_{si}N_a (V_{bi} + V_c(y) - V_b)} \\ &\approx \alpha C_{ox} [2V_{bi} + (V_c(y) - V_b) + \dots] \end{aligned} \quad \alpha = \frac{1}{C_{ox}} \sqrt{\frac{q\varepsilon_{si}N_a}{2V_{bi}}}$$

- Integrate the drain to source current

$$J_{ds} = -\mu_n q_c(y) \frac{\partial V_c}{\partial y} = \frac{1}{L} \int_0^L J_{ds} dy = \frac{\mu_n}{L} \int_{V_s}^{V_d} q_c(V_c) dV_c = \frac{C_{ox} \mu_n}{2(1+\alpha)} (V_{gst}^2 - V_{gdt}^2)$$

## BSIM model substitutions

- At this point the BSIM model changes variables from  $V_{gs}$  and  $V_{gd}$ , to  $V_{gs}$  and  $V_{ds}$ .

$$V_{ds} = V_d - V_s$$

$$V_{gdt} = V_{gst} - (1 + \alpha)V_{ds}$$

- The result is

$$J_{ds} = \frac{C_{ox}\mu_n}{L} \left[ V_{gst} - \frac{(1 + \alpha)V_{ds}}{2} \right] V_{ds}, \quad V_{ds} \geq 0$$

- This destroys the source/drain symmetry when a voltage dependence is added to quantities that have been considered to be constant up to now.

## BSIM modifications that destroy symmetry

- **Threshold voltage:**

$$V_{ts} = V_{t0} + \alpha (2V_{bi} - V_{bs}) \approx V_{t0} + \sqrt{2q\epsilon_{si}N_a (V_{bi} - V_{bs})} + \dots$$

$$J_{ds} = \frac{C_{ox}\mu_n}{L} \left[ \max(V_{gs}, V_{gd}) - V_{t0} - \sqrt{2q\epsilon_{si}N_a (V_{bi} - \max(V_{bs}, V_{bd}))} - \frac{(1+\alpha)|V_{ds}|}{2} \right] V_{dseff}$$

- **Mobility:**  $\mu_n = \mu_n(V_{gst}, V_{bs})$

- **Bulk charge factor:**  $A_{bulk} = (1 + \alpha) = A_{bulk}(V_{gst}, V_{bs})$

- **The  $V_{ds} \approx V_{dseff}$  is not symmetric.**

- **Other**

## Physical Picture for LINFET

- BSIM first integrates the drain to source current, and then makes the parameters  $V_t$ ,  $\mu_n$ , and  $\alpha$  voltage dependent.

$$J_{ds} = \frac{\mu_n}{L} \int_{V_s}^{V_d} q_c(V_c) dV_c = \frac{C_{ox}\mu_n}{2(1+\alpha)} (V_{gst}^2 - V_{gdt}^2) = J_s - J_d$$

- This suggests that we define two opposing currents, with voltage dependent parameters defined at the source and the drain.

$$J_s = \frac{C_{ox}\mu_{ns}}{2(1+\alpha_s)} (V_g - V_s - V_{ts})^2$$

$$J_d = \frac{C_{ox}\mu_{nd}}{2(1+\alpha_d)} (V_g - V_d - V_{td})^2$$

## LINFET approach

- **The current equation is factored.**
  - The  $V_{gst}$  and  $V_{gdt}$  dependence is retained.
  - Notice the fortuitous cancelation of the bulk charge factor **(1 + a)**.

$$J_{ds} = \frac{C_{ox}\mu_n}{2(1+\alpha)L} \left( V_{gst}^2 - V_{gdt}^2 \right) = \frac{C_{ox}\mu_n}{L} \left( \frac{V_{gst} + V_{gdt}}{2} \right) V_{ds}$$

- **We keep two threshold voltage expressions.**

$$V_{ts} = V_{t0} + \alpha (2V_{bi} - V_{bs}) \approx V_{t0} + \sqrt{2q\epsilon_{si}N_a (V_{bi} - V_{bs})} + \dots$$

$$V_{td} = V_{t0} + \alpha (2V_{bi} - V_{bd}) \approx V_{t0} + \sqrt{2q\epsilon_{si}N_a (V_{bi} - V_{bd})} + \dots$$

## LINFET approach (continued)

- The mobility can be handled in two ways.

$$J_{ds} = \frac{C_{ox}}{L} \left( \frac{\mu_{ns} V_{gst} + \mu_{nd} V_{gdt}}{2} \right) V_{dseff}$$

$$\mu_{ns} = \mu_{ns} (V_{gst}, V_{bs})$$

$$\mu_{nd} = \mu_{nd} (V_{gdt}, V_{bd})$$

- Or

$$J_{ds} = \frac{C_{ox}}{L} \left( \mu_{neff} (\mu_{ns}, \mu_{nd}) \right) \left( \frac{V_{gst} + V_{gdt}}{2} \right) V_{dseff}$$

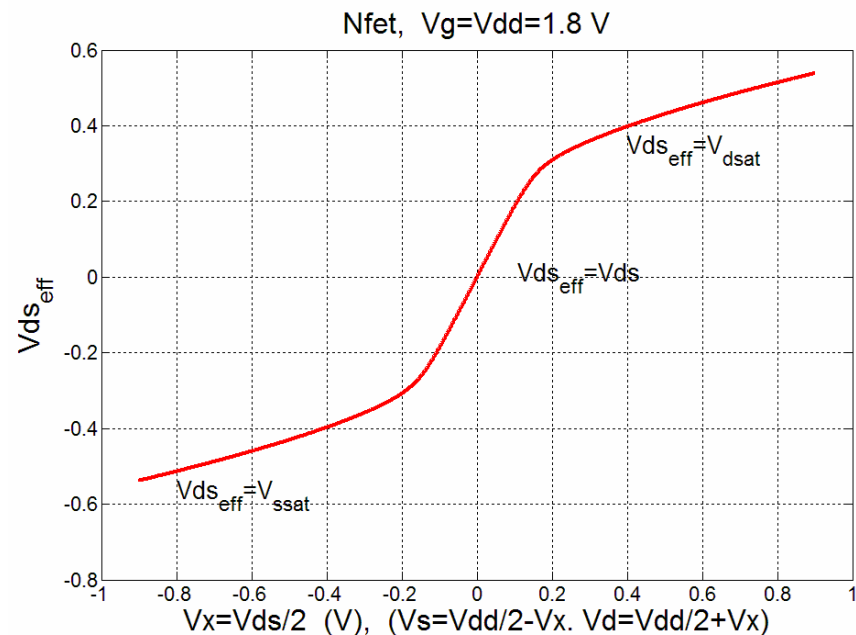
$$\frac{1}{\mu_{neff}} = \frac{1}{2} \left( \frac{1}{\mu_{ns}} + \frac{1}{\mu_{nd}} \right)$$

## LINFET approach (continued)

- The effective  $V_{dseff}$  factor can be written in a symmetric manor.
  - We define two saturation voltages for the source and drain.
  - The  $\delta$  term can be used as a fitting factor.

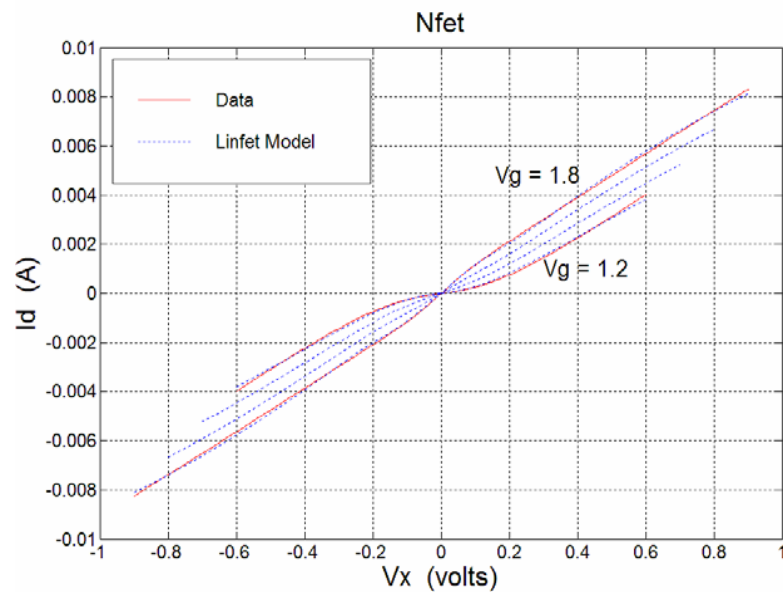
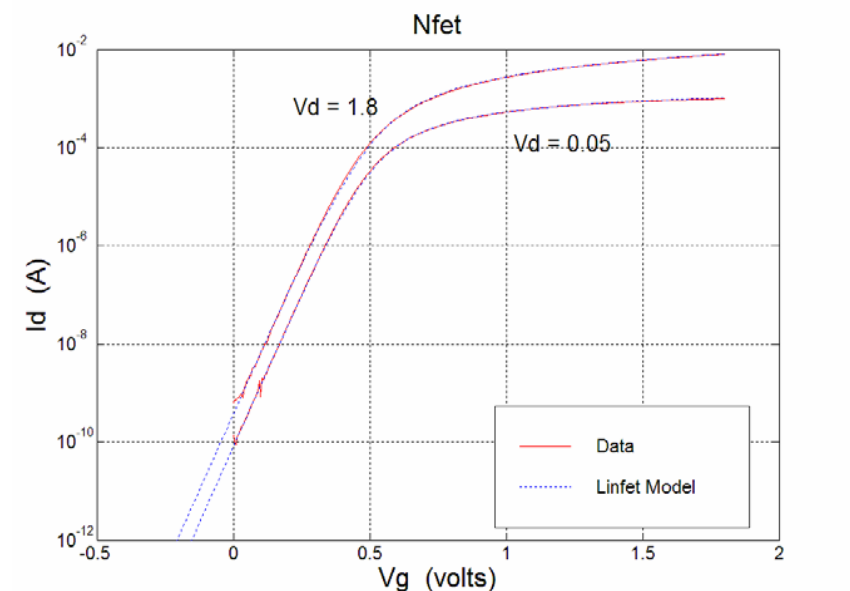
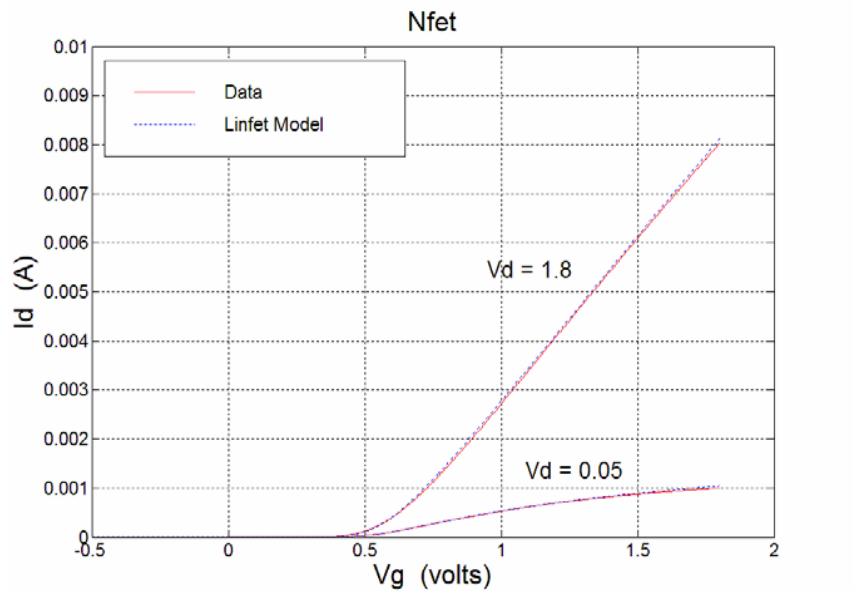
$$V_{dseff} = \frac{1}{2} \left[ V_{dsats} - V_{ssatd} - \sqrt{(V_{dsats} - V_{ds})^2 + 4\delta(V_{dsats} + \delta)} + \sqrt{(V_{ssatd} + V_{ds})^2 + 4\delta(V_{ssatd} + \delta)} \right]$$

$$V_{dsats} = V_{dsat}(V_{gst}), \quad V_{ssatd} = V_{dsat}(V_{gdt})$$



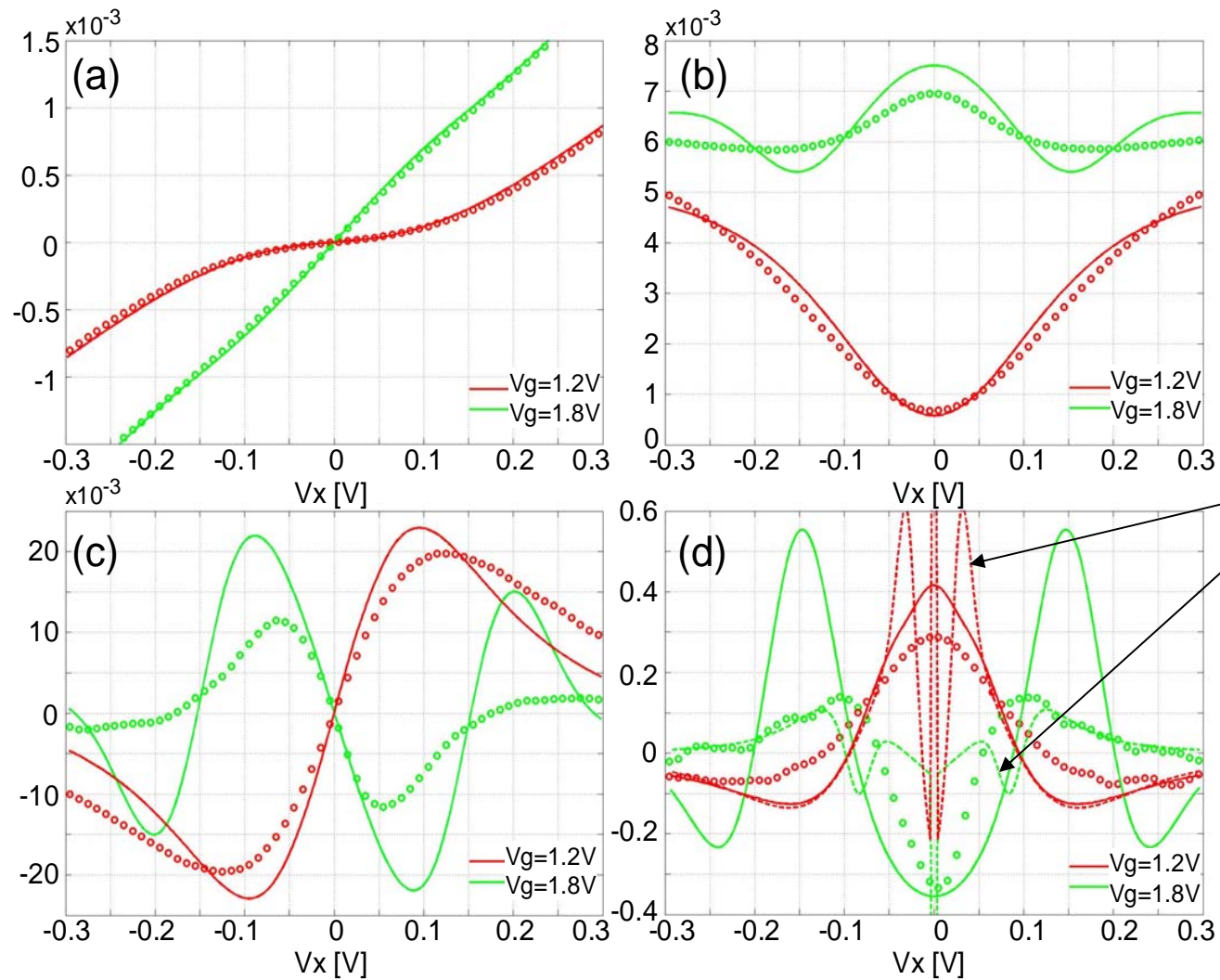
## LINFET approach (continued)

- **Voltage dependent BSIM parameters evaluated at both the drain and the source.**
  - $V_{th}$  Threshold Voltage
  - $\mu_{eff}$  Effective mobility
  - $V_{dsat}$  Saturation voltage
  - $E_{sat}$  Electric field
  - $V_A$  Early voltage
  - $A_{bulk}$  Bulk charge factor



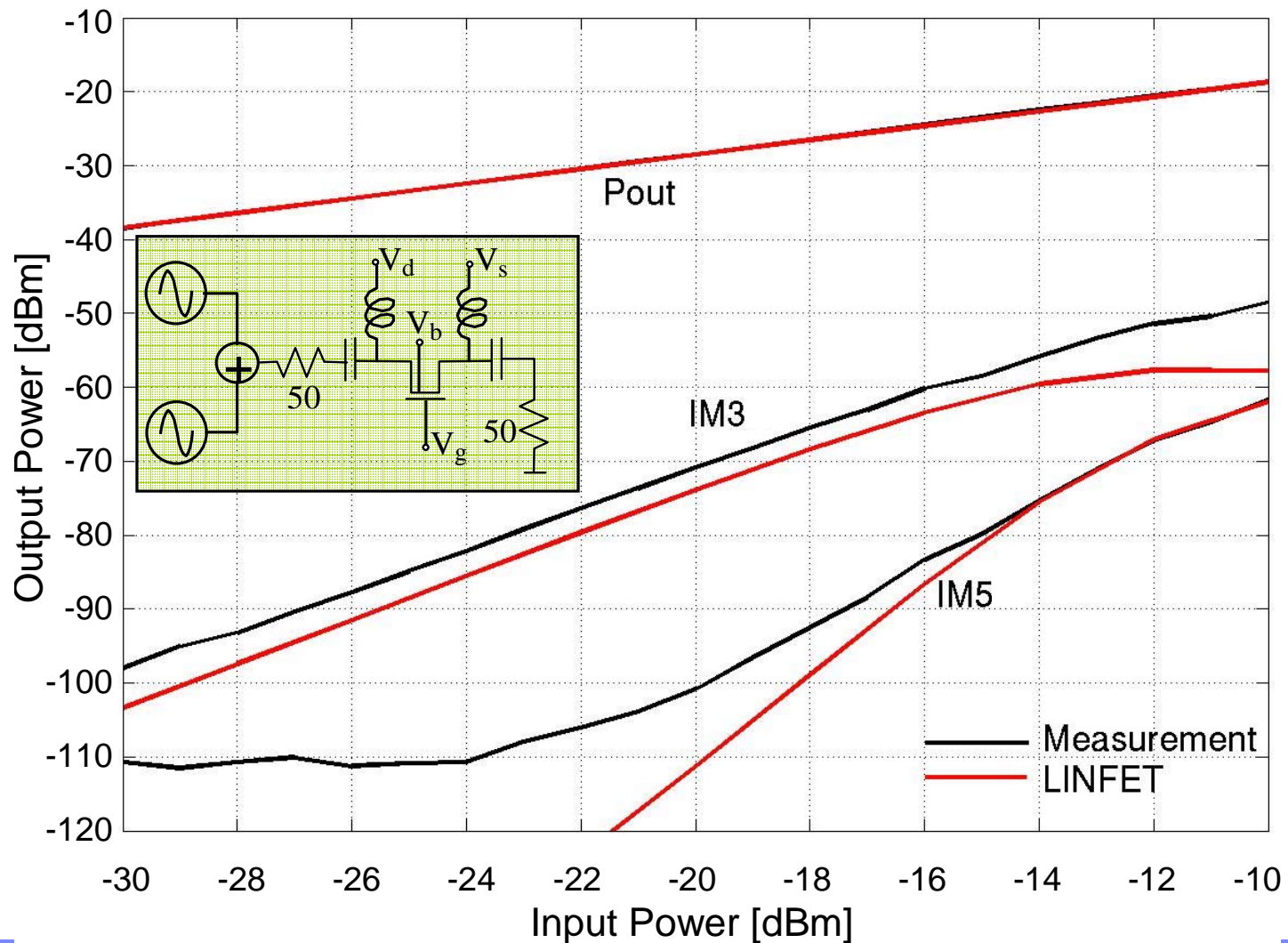
Gummel symmetry test for a  $0.18 \times 10 \mu\text{m}$  NFET.

a) IV, b) 1st derivative, c) 2nd derivative, d) 3rd derivative.



**BSIM**

Distortion in the 3rd (IM3) and 5th (IM5) intermodulation products for a passive mixer configuration.



## LINFET capacitance formulation

- Charges retain dependence on  $V_{gst}$  and  $V_{gdt}$ .

$$Q_c = \int_0^L q_c(y) dy = -\frac{2}{3} C_{ox} L \frac{V_{gst}^3 - V_{gdt}^3}{V_{gst}^2 - V_{gdt}^2} = -\frac{2}{3} C_{ox} L \left( \frac{V_{gst}^2 + V_{gst} V_{gdt} + V_{gdt}^2}{V_{gst} + V_{gdt}} \right)$$

$$Q_g = \int_0^L q_g(y) dy = \frac{C_{ox} L}{(1+\alpha)} \left\{ \alpha (V_{gb} - V_{t0} + 2V_{bi}) + \frac{2}{3} \left( \frac{V_{gst}^2 + V_{gst} V_{gdt} + V_{gdt}^2}{V_{gst} + V_{gdt}} \right) \right\}$$

$$Q_b = \int_0^L q_b(y) dy = -\frac{\alpha C_{ox} L}{(1+\alpha)} \left\{ (V_{gb} - V_{t0} + 2V_{bi}) - \frac{2}{3} \left( \frac{V_{gst}^2 + V_{gst} V_{gdt} + V_{gdt}^2}{V_{gst} + V_{gdt}} \right) \right\}$$

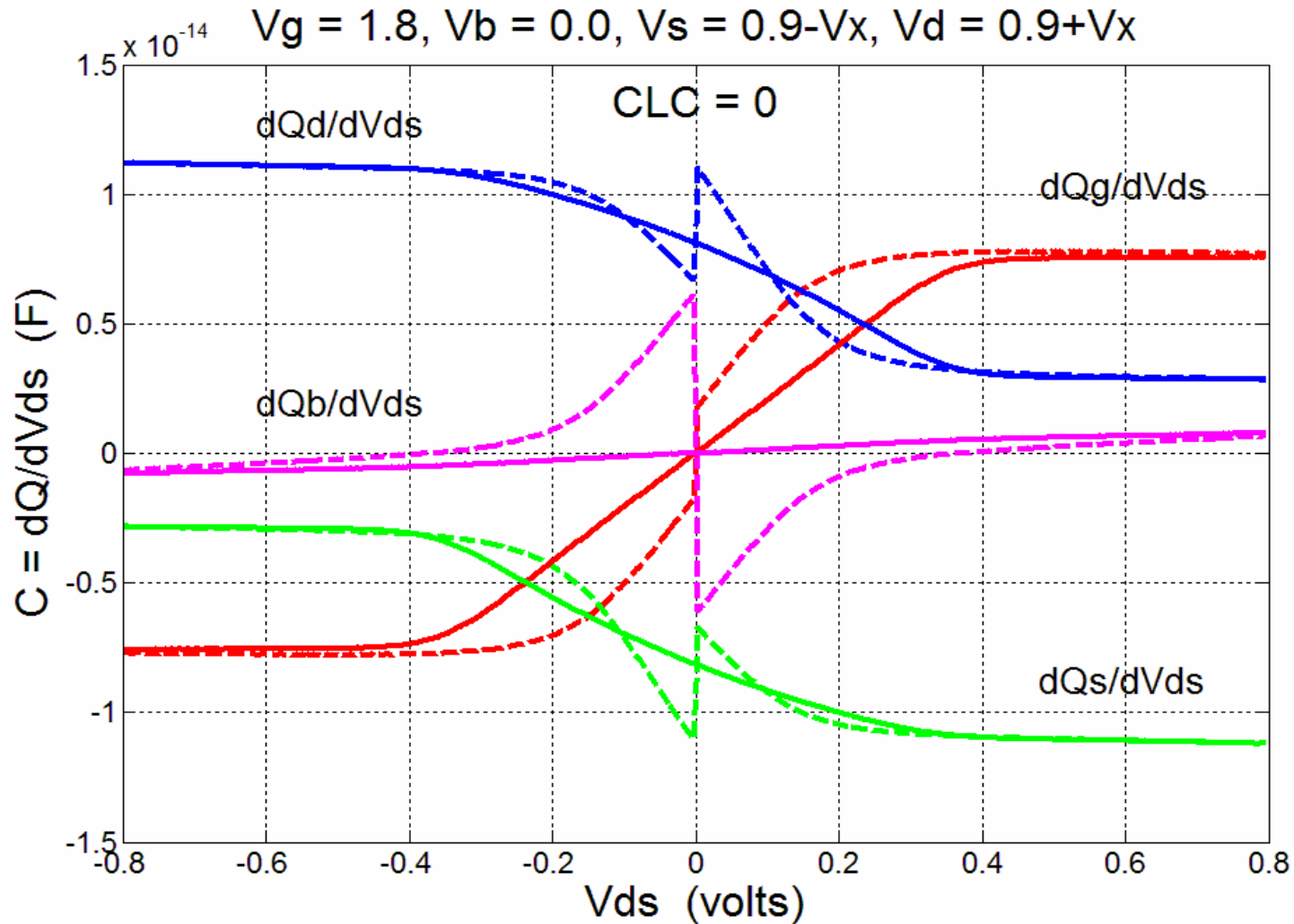
## LINFET capacitance formulation (continued)

- **Source/Drain charges with 40/60 partitioning.**

$$Q_s = \int_0^L q_c(y) \left(1 - \frac{y}{L}\right) dy = -\frac{2}{15} C_{ox} L \left[ \frac{3V_{gst}^3 + 6V_{gst}^2 V_{gdt} + 4V_{gst} V_{gdt}^2 + 2V_{gdt}^3}{(V_{gst} + V_{gdt})^2} \right]$$

$$Q_d = \int_0^L q_c(y) \left(\frac{y}{L}\right) dy = -\frac{2}{15} C_{ox} L \left[ \frac{2V_{gst}^3 + 4V_{gst}^2 V_{gdt} + 6V_{gst} V_{gdt}^2 + 3V_{gdt}^3}{(V_{gst} + V_{gdt})^2} \right]$$

Derivatives of gate, source, drain and body charges.  
 Dashed lines: BSIM model. Solid lines: LINFET model.



## Conclusions

- **The LINFET model removes all the discontinuities in the derivatives of current and charge at  $V_{ds}=0$ .**
  - This result is possible because source/drain symmetry is maintained throughout the model derivation.
  - The derivation parallels that of BSIM so that many of the parameters from existing BSIM models may be reused. Only a minor recentering of the model is necessary.
  - We have shown good agreement between model and hardware up to the third derivative of the drain to source current.